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Computation of Southern Pine Site Index Using a TI-59 Calculator

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SUMMARY

A program is described that permits computation of site index in the field using a Texas Instruments model TI-59 programmable, hand-held, batterypowered calculator. Based on a series of equations developed by R.M. Farrar, Jr., for the site index curves in USDA Miscellaneous Publication 50, the program can accommodate any index base age, tree age, and height within wide limits for the four principal southern pine species: loblolly (*Pinus taeda L.*), longleaf (*P. palustris Mill.*), shortleaf (*P. enchinata Mill.*) and slash pine (*P. elliottii* Engelm.). Small errors in estimating average stand age or height cause large errors in estimating site index, especially for young stands. The program is used to explore the sensitivity of site index estimates to age and height errors.

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INTRODUCTION

Forest management is influenced by the productivity of the tract supporting the timber. Site index — the expected average height of the dominant and codominant stems in a stand at a reference base age — is a measure of the productive capacity of the land for a given species. Traditional methods of computing site index require lengthy calculations back at the office. To determine approximate site index of southern pine stands in the field, foresters have often relied upon ocular interpolation of the curves for index base age 50 presented in Miscellaneous Publication 50 (USDA Forest Service 1976). But ocular interpretation of site index differences for young stands is very difficult and translation to other index base ages is also difficult with the curves.

This report contains a listing of the program for a Texas Instruments model TI-59 calculator¹ that allows foresters to compute site index quickly and accurately in the field. The program also enables foresters to translate indexes to different base ages, to compare expected heights at different ages on the same site, and to compare site indexes implied by differing heights of trees the same age. Finally, a sensitivity analysis of site index estimates is reported that illustrates the inaccuracy resulting from small errors in determining stand age and stand height.

PROGRAM BACKGROUND

Farrar (1973) expressed the site index curves in Miscellaneous Publication 50 as equations having the form:

$$\begin{split} \text{Log(SI)} &= \text{Log(ATH)} + b_1 [\frac{1}{\text{IBA}} - \frac{1}{\text{ATA}}] \\ &+ b_2 [(\frac{1}{\text{IBA}})^2 - (\frac{1}{\text{ATA}})^2] \\ &+ b_3 [(\frac{1}{\text{IBA}})^3 - (\frac{1}{\text{ATA}})^3] \\ &+ b_4 [(\frac{1}{\text{IBA}})^4 - (\frac{1}{\text{ATA}})^4] \end{split}$$

where Log = logarithm, base 10

- SI = site index
- ATH = average total height of the dominant and co-dominant trees in a stand
- IBA = site index base age
- ATA = average total age-from-seed of the dominant and co-dominant trees in the stand

Farrar (1975) later developed a FORTRAN program to calculate site index (or height) arrays from inputs of index base age, average tree age and average height (or site index).

The calculator program presented here (appendix, Program Listing) uses coefficients Farrar (1975) developed to describe site index curves in Miscellaneous Publication 50. Thus, the same limitations regarding age, site index, and average height apply (table 1).

The User Instructions contain five basic steps (appendix). The first step initializes the program's parameters and prepares the calculator for one of the next four steps, each a different program option.

Step 1: Program Initialization

During initialization, the calculator memory is partitioned between storage for program steps and for constants and the program is entered into calculator memory. If the memory is not partitioned properly, the program cannot be loaded. Program

¹The use of trade, firm, or corporation names in this report is for the information and convenience of the reader. Such use does not constitute official endorsement or approval of the product or firm by the USDA to the exclusion of others which may be suitable.

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Table 1.——Limits for species equations¹

	Loblolly	Longleaf	Shortleaf	Slash
Age limits (years)	1080	15-100	10-100	10-60
age 50 (feet)	60-120	40-120	40-100	60-100

¹From Farrar (1975, table 1).

execution begins with the constants for the desired species being retrieved from storage and positioned in the general equation subroutine. The program moves automatically to step 2 after completing initialization.

Step 2: Site Index Calculation

This step, the subroutine labeled E inside the program, automatically calculates the average total age and average total height of the stand at the sampling point from the ages and heights of individual trees. The calculator display prompts the user for data using a numerical code. When the display contains 1111111111, the next datum needed is the site index base age; 2222222222, the tree age; 33333333333, the tree height. Ages and heights for a minimum of 10 dominant and codominant trees should be measured and entered. The display flashes the number of trees already entered before prompting the user for the next age. A zero is entered for tree age after the data for all trees at a sampling point are entered, causing the program to prepare for index calculation. The program asks for the index base age, then computes average age, average height and site index of the stand. The average age and average height flash in the display and site index is displayed. If the calculator is attached to a PC-100 printer, the results are also printed.

From Step 2, the user can branch to any of the next three steps by entering the appropriate letter (A,B, or C). If the calculation of site index is desired at another sample location in the stand, press "RUN/STOP" and the program will recycle and prepare for the first tree age at the next sample location. Previously calculated site indexes, average ages or average heights are not stored in calculator memory. For a different species, go back to step 1.4.

Step 3: Height Projection

This step, the subroutine labeled A inside the program, calculates an expected height for each age specified by the user, given site index and index base age, the inverse of step 2. Step 3 can also be used to convert from one index base age to another. For example, a particular stand of longleaf pine may have a site index of 70, base age 25. At age 50, the dominant and codominant trees would have an average height of 110 feet. Because age 50 can also be considered an index base age, the height at this age becomes the site index — 110 feet.

When the program displays 444444444, enter site index. After entering the age for which height is desired, the program calculates expected height. Press "RUN/STOP" to recycle for another age. All the variables entered are also printed if a PC-100 printer is attached.

Step 4: Height Vector

This step, the subroutine labeled B inside the program, calculates a vector of expected average heights of dominant and codominant trees for a vector of average stand ages. The user specifies site index, base age, and the increment between ages when heights are desired. The program prompts 555555555 for the age increment in years. The program begins at age 10 (15 for longleaf) and continues computing heights for each age until the upper age limit is reached (table 1). When the upper age limit is reached, 9876543210 is displayed. Both the age and height vectors are printed if a PC-100 printer is attached.

Step 5: Site Index Vector

The site index vector, the subroutine labeled C inside the program, is similar to the height vector. The user specifies the stand age, index base age, height increment and the maximum height desired. The program calculates the site index associated with each height, beginning at 10 feet, for the specified average stand age. The program prints 999 for output if site index is less than 10 feet or greater than 170 feet. The end of the vector is marked by 987654321. The height and site index vectors are both printed if a PC-100 printer is attached.

Using the Program

Foresters should thoroughly familiarize themselves with the program before using it in the field the first time. The following 10 operations should be performed.

- 1. Keystroke the program (appendix) into the machine after properly partitioning the memory.
- 2. Write 2 sets of cards for the program.
- 3. Clear the memory.

- 4. Reload the recorded program.
- 5. Run a complete listing (2ND LIST and INV 2ND LIST) of the recorded and reloaded program.
- 6. Verify keystroke accuracy against Program Listing (appendix).
- 7. Correct any mistakes.
- 8. Rewrite both sets of cards, if necessary.
- 9. Run the test problems (appendix) to verify that the program is working properly.
- 10. Use a data set you have previously analyzed and compare the program's results with your prior results.

SENSITIVITY ANALYSIS

Users must bear in mind the age limitations inherent in Miscellaneous Publication 50 (USDA Forest Service 1976). The ages specified for loblolly, shortleaf, and slash pine are ring counts to pith from cores taken at dbh, plus 3 years. For longleaf pine, age is ring count to pith from cores taken at dbh, plus 7 years. All of the data came from naturally regenerated, second-growth stands. Consequently, the ages are all estimated *age-from-seed*. Users should calculate the ages of their trees the same way.

Using the program for plantations can create problems. In the first place, the height growth patterns depicted by the site index curves for natural stands may not match the patterns in plantations, especially

plantations on old field or prepared sites. Assuming that the curves are suitable, there is still another problem. When a plantation is established, the 1-0 (bare-rooted) seedlings planted are already 1 year old from seed. Thus, when a plantation is 25 years old, the trees are actually 26 years from seed. Common practice presumes that the average height of dominant and codominant trees in a plantation 25 growing seasons after planting is the site index with an index base age of 25 years. But this presumption creates a one year height growth error in this program. The height of a stand planted 25 years previously is the site index only if the index base age is 26 or the seedlings planted were grown in containers and were less than 6 months old when planted. Thus, the presumption that average plantation height equals site index is only correct for plantations 24 years after establishment with 1-0 (bare-root) seedlings.

Serious errors are created when evaluating site quality based on young, fast-growing stands if the year's difference in age-from-seed versus age-fromestablishment is ignored. For example, suppose the average height of dominant and codominant trees in a loblolly pine plantation 11 years from seed (10 years after establishment) is 36 feet. Site index, base age 50 for 11 years and height 36 feet is 80. But if the age is mistakenly entered as 10, based on the age since establishment, site index for a height of 36 feet is 96. The error of one year induces a 20 percent error in site index (fig. 1). If these overestimates of



Figure 1.—Site index percentage overestimate resulting from a one-year aging error, $SI_{50} = 80$ for each species.

site index are used as arguments in some stand volume and growth predictors to estimate present and future volumes, they obviously cause overestimates of both volumes and growth. The problem becomes most acute when young, fast-growing stands are on the verge of merchantability and when the log-rule being used, such as the Doyle Rule, penalizes small stems. Under these conditions, overestimating site index by 10 to 20 percent can lead to overestimating future growth and yield by 33 to 50 percent over 20 to 30 year rotations (Feduccia et.al. 1979). Economic evaluations of investments in possible intermediate treatments founded on such overestimates of site index will conclude that higher rates-of-return will be earned than will actually occur. Consequently, landowners may over-invest in stand treatments and inefficiently allocate scarce management funds.

Foresters should take care when comparing their own plantations with published yield tables or with growth and yield models that vary with site index. They should determine whether the published information was constructed using age-from-seed or agefrom-establishment and which age is implied in the site index base age. Then, this program can be used to properly enter the published plantation yield tables or utilize published equations for comparison.

In the authors' experiences, field foresters using clinometers tend to overestimate tree heights by 2 to 10 percent compared to actual heights measured with a tape after felling. It is often difficult to actually see the true tree top because closed crown canopies or intervening branches near the top of the tree can obstruct the measurer's vision. Consequently, heights taller than those actually existing are often recorded. However, in contrast to the misspecification of age, height errors are not compounded. Site index is only raised by the same percentage as the percent height error. The nature of the errors flows directly from the form of the estimating equation. Because ages are used in the exponent of the equation, the equation is much more sensitive to aging errors than height estimation errors. But, overestimating actual heights compounds the problem of determining site index for plantations when the year that seedlings spend in the nursery is ignored.

Sound data collection procedures should eliminate the age and height estimation errors. If accurate data are used, this program will provide site indexes and height growth projections far superior to results from ocular interpolation of curves without having to retreat to the office for computations.

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Appendix

Program Listing

4) 400 43 RCL 5 + 401 14 14 5 + 401 14 14 3 C 403 15 15 3 RCL 403 15 15 3 13 404 43 RCL 5 × 405 00 00 5 × 406 32 XIT 8 RCL 407 43 RCL 8 RCL 407 43 RCL 8 RCL 407 43 RCL 9 99 76 LBL 64 4 410 91 R/S R/S 9 99 413 76 LBL 4 416 39 39 R/A 4 416 39 RPR A117 71 SBR 4 416 39 RPR A22 66 PAU 5 RCL 423 99 PR	Heat Heat Heat 15 -19758.5 ADV -11.8701 SBR 0. PAU 1263.79 × -12409.5 SBR -11.104909 E' -83.244961 = 2239.678 X:T -11260.453 1 -8.80405 0 22.7952 GE 9876543210. GRD 111111111.1 1 222222222.7 7 33333333333.3 0 44444444444. X:T 555555555. GE 6666666666. GRD 777777777. SBR 0. PAU 9999999999. LBL I×I
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User Instructions

Step	Procedure	ENTER	Press	Display
1.0	INITIALIZE THE PROGRAM PARAMETERS	ni da da como a construcción de la		
1.1	Partition the calculator.	6	2ND OP 17	479.59
1.2	Load the program, reading card sides 1 to 4.	side #	INV 2ND WRITE	side #
1.3	Begin execution.		RST R/S	9876543210.
1.4	Select the species desired: $A' = $ loblolly; $B' = $ longleaf;			
	C' = shortleaf; and $D' = $ slash		2ND (letter)	2222222222.
2.0	SITE INDEX CALCULATION ^a			
2.1	Enter the present tree age (PTA).	PTA	R/S	3333333333.
2.2	Enter the present tree height (HT).	\mathbf{HT}	R/S	2222222222.
2.3	Do steps 2.1 and 2.2 for all n sample trees.			
2.4	After entering the last sample tree height, enter 0 for			
	the next PTA.	0	R/S	1111111111.
2.5	Enter the index base age (IBA) desired.	IBA	R/S	Site Index
2.6	To prepare the program for calculating site index at a			
	new sample location. If a new species is desired,		R/S	2222222222.
	go to step 1.4			
3.0	HEIGHT PROJECTION		А	444444444.
3.1	Enter site index (SI).	\mathbf{SI}	R/S	1111111111.
3.2	Enter index base age (IBA).	IBA	R/S	22222222222.
3.3	Enter the stand age (SA).	\mathbf{SA}	R/S	Expected HT
3.4	Recycle the program for the next stand age.		R/S	22222222222.
4.0	HEIGHT VECTOR		В	444444444.
4.1	Enter site index (SI).	SI	R/S	1111111111.
4.2	Enter index base age (IBA).	IBA	R/S	5555555555.
4.3	Enter age increment (AI). The program continues until upper age limits are reached.	AI	R/S	Ages & Heights 9876543210.
5.0	SITE INDEX VECTOR		С	1111111111.
5.1	Enter index base age (IBA)	IBA	R/S	2222222222.
5.2	Enter the average tree age (ATA)	ATA	R/S	6666666 66 .
5.3	Enter height increment (HTI).	HTI	R/S	7777777777.
5.4	Enter maximum height (HTMAX). The program continues	HTMAX	R/S	Heights and
	to HTMAX. If an SI outside the range $10 < SI < 170$			Site Indexes
	is computed, the program prints 99999999999. The end			
	is marked 987654321.			987654321.

"To get to step 2.0 without going through step 1, press E from anywhere in the program.

Program Test Problems

Step	Action	Printer tape	Calculator display
1.0	Initialize the program		
1.1	Partition the calculator		479.59
1.2	Load the program by reading cards		1,2,3,4
1.3	Begin execution		9876543210.
1.4	Select loblolly pine (A')		22222222222.
2.0	Calculate site index using the data (E)		
2.1	PTA — 16,15,18,17,16,17,15,16,16,17		3333333333.
2 .2	HT – 47,42,51,47,43,48,43,45,44,49	1, 2,	1,2,, 10. &
2.3	Repeat 2.1 and 2.2 for all 10 trees	, 10	22222222222.
2.4	Enter 0 for PTA after $HT = 49$		1111111111.
2.5	Enter IBA $= 25$	25	
	Display flashes the average age.	16	16
	Display flashes the average height:	46	46
	Display stops flashing, SI appears:	68	68
3.0	Calculate expected stand heights (A)		444444444.
3.1	Enter $SI = 80$	80	1111111111.
3.2	Enter $IBA = 25$	25	22222222222.
3.3	Enter $SA = 18$	18	
	Expected height is displayed	60	60
3.4	Recycle for next SA: R/S		22222222222.
3.3	Enter $SA = 27$	27	
	Expected height is displayed	85	85
4.0	Calculate a height vector (B)		444444444.
4.1	Enter $SI = 70$	70	1111111111.
4.2	Enter IBA $= 30$	30	55555555555.
4.3	Enter $AI = 10$	10	
	The display flashes	$PTA = 10 \ 20 \ 30 \ 40$	50 60 70 80
	and printer prints:	HT = 23 50 70 84	93 100 104 108
	The end marker appears:	9876543210.	9876543210.
5.0	Calculate an SI vector (C)		11111111111.
5.1	Enter IBA $= 50$	50	22222222222.
5.2	Enter $ATA = 67$	67	666666666.
5.3	Enter $HTI = 20$	20	7777777777.
5.4	Enter HTMAX $= 200$	200	
	The display flashes	$HT = 10 \ 30 \ 50 \ 70 \ 90 \ 110$	130 150 170 190
	and printer prints:	$SI = 999 \ 27 \ 45 \ 63 \ 81 \ 100$	118 136 154 999
	The end marker appears:	9876543210.	9876543210.

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A program is described that permits computation of site index in the field using a Texas Instruments model TI-59 programmable, hand-held, battery-powered calculator. Based on a series of equations developed by R.M. Farrar, Jr., for the site index curves in USDA Miscellaneous Publication 50, the program can accomodate any index base age, tree age, and height within wide limits for four principal southern pine species.

Keywords: Growth, timber management, loblolly pine, longleaf pine, shortleaf pine, slash pine, computer program, plantation, dendrochronology.