

DIAMETER DISTRIBUTIONS IN NATURAL YELLOW-POPLAR STANDS

by

Charles E. McGee and Lino Della-Bianca



Cover photo: A Southern Appalachian yellow-poplar stand with a wide variety of diameters.

Southeastern Forest Experiment Station
Asheville, North Carolina
Forest Service
U.S. Department of Agriculture

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Charles E. McGee, **Silviculturist**

and

Lino Della-Bianca, **Associate Silviculturist**

EXCELLENT STANDS of yellow-poplar grow on fertile, well-drained coves, lower slopes, and bottom lands in the Southern Appalachian mountains. These elite stands make up only a small portion of the mountain forest, but, because of their productivity, they are of great importance to the mountain economy.

Foresters and timber owners need information that will help them plan the intensive management these stands should have. This paper presents the diameter distributions found in pure, unthinned stands of yellow-poplar. These distributions represent the natural development of the number of trees in specific size classes in relation to stand age, site index, and total number of stems per acre. If what has happened in the past is a good indicator of what will happen *in the future*, the stand descriptions should be very valuable for answering questions that must be decided in stand management planning. For instance, will it pay to thin a yellow-poplar stand on a moderate site at age 30, or will the trees be thinned be too small to make a merchantable cut? Of course, in yellow-poplar stands the production of high-value veneer logs outweighs most every other consideration. Therefore, another important question is, will there be enough veneer-size stems on the site at age 60 to justify a harvest cut, or will the number of veneer-size trees increase enough to warrant waiting until age 70?

Admittedly, these data will not answer all questions, and someday more accurate criteria based on remeasurement of managed stands will probably become available. Meanwhile, the value of these diameter distributions is already being proved.

Methods

Plot Selection

Data for this study were obtained from 141 circular $\frac{1}{4}$ -acre plots established in the Appalachian Mountains of North Carolina (93 plots), Virginia (31 plots), and Georgia (17 plots). Site index, stand age, and number of trees per acre, by 1-inch diameter classes, were obtained **on each plot**.

To be included **in** the study, a stand had to have 75 percent or more of its overstory in yellow-poplar. All the stands were even-aged and ranged from 17 **to 76** years of age. Site index at age 50 ranged from 7.5 to 150 feet, and basal area varied from 44 to 208 square feet per acre. The maximum and minimum number of yellow-poplar trees per acre, by stand age and site index, are shown in table 1.

Sampled stands were free of disease and insects and showed no evidence of past cutting. Trees were well distributed over the plot.

TABLE 1.—Minimum and maximum observed numbers of yellow-poplar trees per acre by age and site index classes.

| Site index (Feet at age 50) | Age (years) | | | | | | |
|-----------------------------------|-------------|-------|-------|-------|-------|-------|------|
| | < 21 | 21-30 | 31-40 | 41-50 | 51-60 | 61-70 | > 70 |
| < 81 | | | | 220 | | | |
| | | | | 220 | | | |
| 81-90 | | 228 | 240 | | 140 | 72 | |
| | | 228 | 320 | | 168 | 196 | |
| 91-100 | | 160 | 256 | 100 | 96 | 72 | 68 |
| | | 380 | 256 | 172 | 208 | 232 | 140 |
| 101-110 | | 176 | 136 | 48 | 84 | 100 | |
| | | 364 | 252 | 272 | 272 | 192 | |
| 111-120 | | 152 | 152 | 136 | 132 | 88 | |
| | | 252 | 332 | 212 | 156 | 176 | |
| 121-130 | 216 | 236 | 124 | 96 | 152 | 136 | |
| | 216 | 396 | 256 | 188 | 152 | 136 | |
| 131-140 | | 164 | 140 | | | | |
| | | 328 | 204 | | | | |
| > 140 | 184 | | | | | | |
| | 184 | | | | | | |

Analysis

Analysis of the data to determine diameter distributions followed procedures developed by Clutter and Bennett for planted slash pine.*

Our objective was to present a table of the number of trees per acre by 1-inch diameter classes for various combinations of age, site index, and total number of trees per acre. Basal area per acre was used in the initial computations, rather than number of trees, because basal area allowed a more accurate description of the number of trees in the larger diameter classes.

The curve form used to determine the proportion of basal area for trees in any 1-inch diameter class was:

$$f(D_i) = \frac{\Gamma(\alpha + \beta + 2)}{\Gamma(\alpha + 1) \Gamma(\beta + 1)} \left(\frac{D_i - D_{min}}{D_{max} - D_{min}} \right)^\alpha \left(1 - \frac{D_i - D_{min}}{D_{max} - D_{min}} \right)^\beta$$

where,

$f(D_i)$ = relative frequency of basal area per acre for diameter D_i ;

α and β = parameters to be estimated from the data;

D_{max} = maximum diameter of trees in the stand;

D_{min} = minimum diameter of trees in the stand (D_{min} was set at 4.5 inches, the smallest trees measured).

* Clutter, Jerome L., and Bennett, Frank A. Diameter distributions in old-field slash pine plantations. Ga. Forest Res. Council. Rep. 13, 9 pp., illus. 1965.

The basal area in any 1-inch diameter class was converted to number of trees per class per acre by the relationship:

$$N_i = P_i \frac{BA}{B_i}$$

where,

N_i = number of trees in the i^{th} diameter class;

P_i = proportion of the total basal area per acre that lies in the i^{th} diameter class ($i = 5, 6, \dots, 27$);

BA = total basal area per acre;

B_i = basal area per tree for the midpoint tree in the i^{th} diameter class ($i = 5, 6, \dots, 27$).

The predicted values of α , β , and D_{max} were obtained from the following equation:

$$\hat{\alpha} = 13.02839 - 0.02546 (\text{Age}) - \left(\frac{66.84692}{\text{Age}} \right)$$

-4.43671 (Logarithm of number of trees)

$$-0.04678 \left(\frac{\text{Site index} \times \text{number of trees}}{1000} \right)$$

$R^2 = 0.476$ Standard error = 0.582

$$\hat{\beta} = 1.21499 - 0.12504 \left(\frac{\text{Age} \times \text{site index}}{1000} \right)$$

$R^2 = 0.129$ Standard error = 0.450

$$\hat{D}_{max} = 9.38123 + 2.41398 \left(\frac{\text{Age} \times \text{site index}}{1000} \right)$$

$$-0.35928 \left(\frac{\text{Age} \times \text{number of trees}}{1000} \right)$$

$R^2 = 0.700$ Standard error = 2.09

Actual values of α , β , and D_{max} were plotted over calculated values. No bias was apparent in any case.

Results and Discussion

The expected number of trees by 1-inch diameter classes was calculated for various combinations of age, site index, and total number of trees per acre. These values are presented in tables 2 through 6. Although the tables are useful, they have several limitations. Neither the tables nor the equations involved in their development describe changes in basal area and number of trees that occur on a given site with time. Such changes can be determined only by periodic remeasurements of permanent plots. To apply the tables, one must assume that a certain number of trees per acre will be present at a given time.

We also recognize that managed stands of the future will not have diameter distributions exactly like those reported here for unmanaged stands, because cleanings and thinnings will remove smaller size classes. It is to be hoped there will be more large trees than are shown in the tables.

TABLE 4.—Diameter distributions for pure natural yellow-poplar stands by age and stand density per acre on site index 110.

| Total trees (Number) | Basal area (Square feet) | Number of trees per diameter class (inches) | | | | | | | | | | | | | | | | | | | | | | | | | |
|-------------------------|-----------------------------|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|--|--|--|
| | | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 | | | |
| Age 20 | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 100 | 37 | 11 | 18 | 18 | 16 | 13 | 10 | 7 | 5 | 2 | | | | | | | | | | | | | | | | | |
| 150 | 44 | 38 | 35 | 26 | 19 | 13 | 9 | 6 | 3 | 1 | | | | | | | | | | | | | | | | | |
| 200 | 50 | 74 | 48 | 30 | 20 | 13 | 8 | 5 | 2 | -- | | | | | | | | | | | | | | | | | |
| 250 | 56 | 113 | 58 | 34 | 20 | 12 | 7 | 4 | 2 | -- | | | | | | | | | | | | | | | | | |
| 300 | 63 | 150 | 68 | 37 | 21 | 13 | 7 | 3 | 1 | -- | | | | | | | | | | | | | | | | | |
| 350 | 72 | 184 | 78 | 41 | 23 | 13 | 7 | 3 | 1 | -- | | | | | | | | | | | | | | | | | |
| Age 30 | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 300 | 60 | 2 | 6 | 10 | 12 | 13 | 13 | 12 | 11 | 9 | 7 | 4 | 1 | | | | | | | | | | | | | | |
| 150 | 74 | 8 | 2 | 7 | 2 | 0 | 2 | 1 | 2 | 0 | 1 | 8 | 1 | 5 | 1 | 2 | 1 | 0 | 6 | 3 | -- | | | | | | |
| 200 | 86 | 1 | 8 | 3 | 0 | 3 | 2 | 2 | 9 | 2 | 5 | 2 | 1 | 1 | 7 | 1 | 3 | 9 | 5 | 1 | -- | | | | | | |
| 250 | 97 | 31 | 44 | 42 | 36 | 30 | 24 | 18 | 13 | 8 | 4 | | | | | | | | | | | | | | | | |
| 300 | 107 | 45 | 59 | 52 | 43 | 35 | 26 | 19 | 13 | 7 | 1 | | | | | | | | | | | | | | | | |
| 350 | 117 | 59 | 72 | 63 | 51 | 39 | 29 | 20 | 12 | 5 | | | | | | | | | | | | | | | | | |
| Age 40 | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 50 | 54 | -- | -- | 1 | 2 | 2 | 3 | 4 | 5 | 5 | 6 | 6 | 6 | 5 | 4 | 1 | | | | | | | | | | | |
| 100 | 83 | 1 | 3 | 5 | 7 | 9 | 10 | 10 | 11 | 10 | 10 | 9 | 7 | 5 | 3 | -- | | | | | | | | | | | |
| 150 | 104 | 3 | 9 | 13 | 15 | 16 | 16 | 16 | 15 | 13 | 12 | 10 | 7 | 4 | 1 | -- | | | | | | | | | | | |
| 200 | 117 | 8 | 18 | 23 | 24 | 24 | 22 | 20 | 18 | 15 | 12 | 9 | 6 | 1 | -- | | | | | | | | | | | | |
| 250 | 129 | 15 | 29 | 33 | 33 | 30 | 27 | 24 | 20 | 16 | 12 | 8 | 3 | | | | | | | | | | | | | | |
| 300 | 142 | 23 | 40 | 43 | 41 | 37 | 32 | 27 | 22 | 17 | 12 | 6 | | | | | | | | | | | | | | | |
| 350 | 154 | 30 | 51 | 53 | 50 | 44 | 38 | 31 | 24 | 17 | 10 | 2 | | | | | | | | | | | | | | | |
| Age 50 | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 50 | 70 | -- | -- | -- | 1 | 1 | 2 | 3 | 3 | 4 | 4 | 5 | 5 | 5 | 5 | 4 | 3 | | | | | | | | | | |
| 100 | 109 | -- | 2 | 3 | 5 | 6 | 7 | 8 | 8 | 9 | 9 | 9 | 8 | 8 | 7 | 6 | 4 | 1 | | | | | | | | | |
| 150 | 131 | 2 | 6 | 9 | 12 | 13 | 13 | 14 | 13 | 13 | 12 | 11 | 10 | 9 | 7 | 5 | 1 | -- | | | | | | | | | |
| 200 | 148 | 5 | 13 | 17 | 19 | 20 | 20 | 19 | 17 | 16 | 14 | 13 | 11 | 8 | 6 | 2 | -- | | | | | | | | | | |
| 250 | 161 | 10 | 22 | 26 | 27 | 27 | 25 | 23 | 21 | 19 | 16 | 14 | 11 | 7 | 2 | -- | | | | | | | | | | | |
| 300 | 175 | 16 | 30 | 35 | 35 | 34 | 31 | 28 | 24 | 21 | 18 | 14 | 10 | 4 | -- | | | | | | | | | | | | |
| Age 60 | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 50 | 89 | -- | -- | -- | 1 | 1 | 1 | 2 | 2 | 2 | 3 | 3 | 4 | 4 | 4 | 4 | 5 | 4 | 4 | 4 | 2 | | | | | | |
| 100 | 133 | -- | 2 | 5 | 12 | 4 | 5 | 6 | 6 | 7 | 7 | 8 | 8 | 7 | 6 | 4 | 1 | | | | | | | | | | |
| 150 | 161 | 2 | 5 | 12 | 4 | 5 | 6 | 6 | 6 | 6 | 6 | 6 | 6 | 5 | 5 | 3 | -- | | | | | | | | | | |
| 200 | 177 | 4 | 11 | 15 | 16 | 17 | 17 | 16 | 16 | 15 | 14 | 13 | 12 | 10 | 9 | 8 | 6 | 1 | -- | | | | | | | | |
| 250 | 190 | 9 | 19 | 22 | 24 | 23 | 22 | 21 | 20 | 18 | 16 | 15 | 13 | 11 | 9 | 7 | 1 | -- | | | | | | | | | |
| Age 70 | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 50 | 109 | -- | -- | -- | -- | 1 | 1 | 1 | 1 | 2 | 2 | 2 | 3 | 3 | 3 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 3 | | | | |
| 100 | 359 | -- | 2 | 5 | 12 | 3 | 4 | 5 | 6 | 6 | 6 | 6 | 6 | 6 | 5 | 5 | 3 | -- | | | | | | | | | |
| 150 | 184 | 2 | 5 | 12 | 3 | 4 | 5 | 6 | 6 | 6 | 6 | 6 | 6 | 5 | 5 | 3 | -- | | | | | | | | | | |
| 200 | 209 | 4 | 10 | 13 | 14 | 15 | 15 | 14 | 14 | 13 | 13 | 12 | 11 | 10 | 10 | 9 | 8 | 7 | 6 | 2 | -- | | | | | | |
| 250 | 220 | 9 | 17 | 20 | 21 | 21 | 20 | 19 | 18 | 16 | 15 | 14 | 13 | 12 | 11 | 9 | 8 | 6 | 1 | -- | | | | | | | |

TABLE 5.—Diameter distributions for pure natural yellow-poplar stands by age and stand density per acre on site index 120.

| Total trees (Number) | Basal area (Square feet) | Number of trees per diameter class (inches) | | | | | | | | | | | | | | | | | | | | | | | | | |
|----------------------|--------------------------|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|---|---|---|
| | | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 | | | |
| Age 20 | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 100 | 39 | 10 | 17 | 17 | 16 | 13 | 10 | 8 | 5 | 3 | 1 | | | | | | | | | | | | | | | | |
| 150 | 46 | 33 | 33 | 26 | 20 | 15 | 10 | 7 | 4 | 2 | -- | | | | | | | | | | | | | | | | |
| 200 | 54 | 64 | 47 | 32 | 22 | 15 | 10 | 6 | 3 | 1 | -- | | | | | | | | | | | | | | | | |
| 250 | 62 | 97 | 59 | 37 | 23 | 15 | 9 | 6 | 3 | 1 | -- | | | | | | | | | | | | | | | | |
| 300 | 70 | 128 | 70 | 42 | 26 | 16 | 10 | 6 | 2 | -- | -- | | | | | | | | | | | | | | | | |
| 350 | 80 | 154 | 82 | 48 | 29 | 18 | 11 | 6 | 2 | -- | -- | | | | | | | | | | | | | | | | |
| Age 30 | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 100 | 67 | 1 | 5 | 8 | 10 | 12 | 12 | 12 | 11 | 10 | 8 | 6 | 4 | 1 | | | | | | | | | | | | | |
| 150 | 82 | 6 | 15 | 18 | 19 | 19 | 18 | 16 | 13 | 11 | 8 | 5 | 2 | -- | | | | | | | | | | | | | |
| 200 | 95 | 14 | 26 | 29 | 28 | 25 | 22 | 18 | 15 | 11 | 8 | 4 | -- | -- | | | | | | | | | | | | | |
| 250 | 108 | 24 | 38 | 39 | 35 | 31 | 26 | 21 | 16 | 11 | 7 | 2 | -- | -- | | | | | | | | | | | | | |
| 330 | 121 | 34 | 50 | 49 | 43 | 36 | 30 | 23 | 17 | 11 | 6 | 1 | -- | -- | | | | | | | | | | | | | |
| 350 | 134 | 42 | 62 | 59 | 52 | 43 | 34 | 26 | 18 | 11 | 3 | -- | -- | -- | | | | | | | | | | | | | |
| Age 40 | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 50 | 59 | -- | -- | 1 | 1 | 2 | 3 | 3 | 4 | 5 | 5 | 6 | 5 | 5 | 4 | 1 | | | | | | | | | | | |
| 100 | 93 | 1 | 2 | 4 | 6 | 8 | 9 | 9 | 10 | 10 | 9 | 8 | 7 | 5 | 3 | -- | | | | | | | | | | | |
| 350 | 114 | 2 | 8 | 11 | 14 | 15 | 15 | 15 | 14 | 13 | 12 | 11 | 9 | 7 | 4 | -- | | | | | | | | | | | |
| 200 | 133 | 6 | 15 | 19 | 21 | 22 | 21 | 20 | 18 | 16 | 14 | 12 | 9 | 6 | 1 | -- | | | | | | | | | | | |
| 250 | 148 | 11 | 23 | 28 | 29 | 29 | 27 | 24 | 22 | 19 | 15 | 12 | 8 | 3 | -- | -- | | | | | | | | | | | |
| 300 | 163 | 16 | 32 | 37 | 38 | 36 | 32 | 29 | 25 | 21 | 16 | 12 | 6 | -- | -- | -- | | | | | | | | | | | |
| 350 | 180 | 20 | 40 | 46 | 46 | 43 | 39 | 34 | 29 | 23 | 17 | 11 | 2 | -- | -- | -- | | | | | | | | | | | |
| Age 50 | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 50 | 79 | -- | 1 | 3 | 4 | 5 | 6 | 7 | 8 | 8 | 8 | 8 | 8 | 7 | 5 | 5 | 5 | 5 | 4 | 3 | 1 | -- | | | | | |
| 100 | 122 | 1 | 5 | 8 | 10 | 11 | 12 | 12 | 12 | 12 | 11 | 11 | 10 | 9 | 7 | 5 | 2 | -- | -- | -- | -- | | | | | | |
| 150 | 149 | 4 | 10 | 14 | 16 | 17 | 18 | 17 | 17 | 16 | 15 | 14 | 12 | 11 | 9 | 7 | 3 | -- | -- | -- | -- | | | | | | |
| 200 | 172 | 7 | 17 | 21 | 24 | 24 | 23 | 22 | 21 | 19 | 18 | 16 | 14 | 11 | 8 | 4 | -- | -- | -- | -- | -- | | | | | | |
| 250 | 188 | 10 | 23 | 29 | 31 | 31 | 29 | 28 | 26 | 23 | 20 | 18 | 15 | 11 | 6 | -- | -- | -- | -- | -- | -- | | | | | | |
| 300 | 206 | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Age 60 | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 50 | 98 | -- | -- | -- | 1 | 1 | 1 | 1 | 2 | 2 | 3 | 3 | 3 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 3 | | | | | | |
| 100 | 154 | 1 | 2 | 3 | 4 | 4 | 5 | 6 | 6 | 6 | 7 | 7 | 7 | 7 | 7 | 6 | 6 | 5 | 4 | -- | w | | | | | | |
| 150 | 185 | 1 | 4 | 6 | 8 | 9 | 10 | 10 | 10 | 10 | 10 | 10 | 10 | 9 | 9 | 9 | 8 | 7 | 6 | 4 | -- | -- | | | | | |
| 200 | 208 | 3 | 8 | 12 | 14 | 14 | 15 | 15 | 15 | 14 | 14 | 13 | 12 | 11 | 11 | 10 | 8 | 7 | 4 | -- | -- | -- | | | | | |
| Age 70 | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 50 | 121 | -- | -- | -- | -- | 1 | 1 | 1 | 1 | 2 | 2 | 2 | 3 | 3 | 3 | 3 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 |
| 100 | 189 | -- | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 | 5 | 5 | 6 | 6 | 6 | 6 | 6 | 6 | 6 | 5 | 5 | 2 | | | | | |
| 150 | 223 | 1 | 3 | 5 | 7 | 7 | 8 | 8 | 9 | 9 | 9 | 9 | 9 | 8 | 8 | 8 | 8 | 7 | 7 | 6 | 5 | 1 | -- | | | | |

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